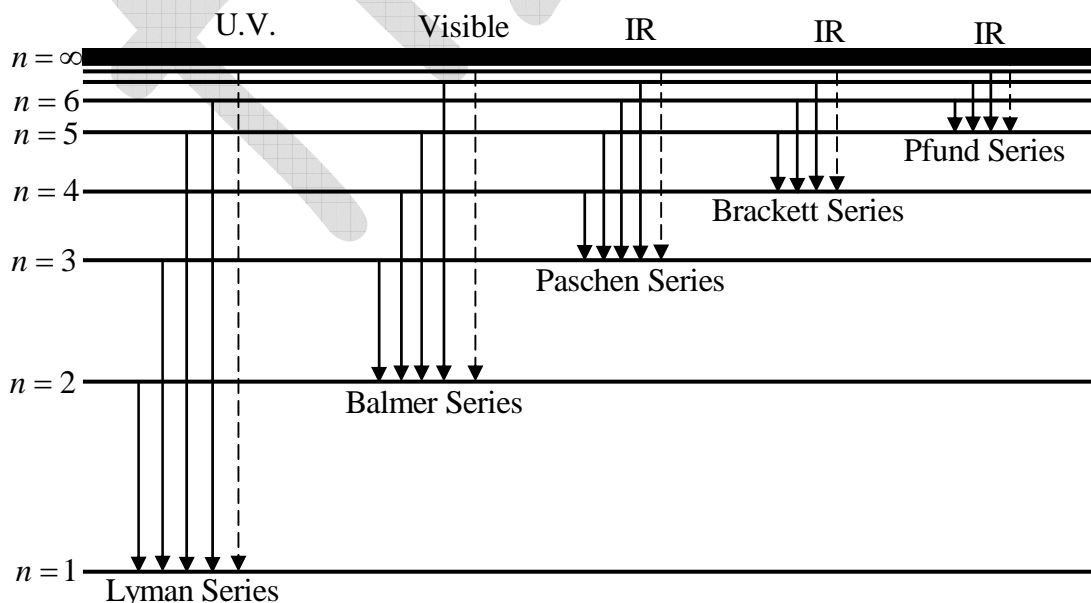


(b) Spectrum of Atomic Hydrogen

It has been discovered that when atoms exposed to white light can absorb light at certain discrete frequencies known as absorption lines or when atoms are excited by the passage of an electric current or by some another means produces discrete frequencies of light known as emission line. The spectrum of light absorbed or emitted by an element is carrying the signature of that element, e.g. Sodium burning in flame, produces two distinct yellow light of wavelength 5896\AA and 5890\AA which is observed after being dispersed by a suitable spectrometer. Each of the wavelength components is called a spectral line and whole family of lines is called a line spectrum. No two different elements can produce similar spectrum. The fact that each element produces its own characteristic spectrum, is of great importance as this information can be used for the chemical or element analysis, for example the elements present in Sun are analysed by this means. J. Balmer (1885) and J. Rydberg (1888) found that the spectral lines in hydrogen atom obey the following mathematical formula

$$\nu = \frac{1}{\lambda} = R \left(\frac{1}{n_f^2} - \frac{1}{n_i^2} \right)$$

Where ν is the frequency of either an emission or absorption line, n_i and n_f are positive integer with $n_i > n_f$ and R is a constant, known as Rydberg's constant.



In atomic hydrogen, different line series are observed which are described below:

(i) **Lyman Series:** The series with $n_f = 1$ is known as the Lyman series and lies in the ultraviolet part of the spectrum.

$$\frac{1}{\lambda} = R \left(\frac{1}{1^2} - \frac{1}{n_i^2} \right) \quad n_i = 2, 3, 4, \dots$$

The lines are labeled as $L_\alpha, L_\beta, L_\gamma, \dots$ in order of decreasing wavelengths.

$$L_\alpha \text{ line: } n_f = 1 \text{ and } n_i = 2; \quad \lambda = 1216 \text{ \AA}$$

$$L_\beta \text{ line: } n_f = 1 \text{ and } n_i = 3; \quad \lambda = 1026 \text{ \AA}$$

$$L_\gamma \text{ line: } n_f = 1 \text{ and } n_i = 4; \quad \lambda = 973 \text{ \AA}$$

While the Lyman series limit ($n_i \rightarrow \infty$) is $\lambda = 912 \text{ \AA}$.

(ii) **Balmer Series:** Balmer series ($n_f = 2$) was first to be discovered and it lies in the visible part of electromagnetic spectrum.

$$\frac{1}{\lambda} = R \left(\frac{1}{2^2} - \frac{1}{n_i^2} \right) \quad n_i = 3, 4, 5, \dots$$

The lines are labeled as $H_\alpha, H_\beta, H_\gamma, \dots$ in order of decreasing wavelengths.

$$H_\alpha \text{ line: } n_f = 2 \text{ and } n_i = 3; \quad \lambda = 6563 \text{ \AA}$$

$$H_\beta \text{ line: } n_f = 2 \text{ and } n_i = 4; \quad \lambda = 4861 \text{ \AA}$$

$$H_\gamma \text{ line: } n_f = 2 \text{ and } n_i = 5; \quad \lambda = 4340 \text{ \AA}$$

While the Balmer series limit ($n_i \rightarrow \infty$) is $\lambda = 3646 \text{ \AA}$. The H_α is an important line used in the detection of hydrogen presence.

(iii) **Paschen Series:** Paschen series was observed by Friedrich Paschen in 1908 corresponds to the transition between the states with ($n_f = 3$) and successive higher states and lies in the near Infrared region of the spectrum.

$$\frac{1}{\lambda} = R \left(\frac{1}{3^2} - \frac{1}{n_i^2} \right) \quad n_i = 4, 5, 6, \dots$$

The Paschen series starts with a line at $18751\overset{\circ}{\text{Å}}$ and ends at $8204\overset{\circ}{\text{Å}}$ (wavelength of Paschen series limit).

(iv) **Brackett Series:** In the Brackett series electron transition takes place from any higher principle quantum state to $n_f = 4$ and it is obtained in the far infrared region.

$$\frac{1}{\lambda} = R \left(\frac{1}{4^2} - \frac{1}{n_i^2} \right) \quad n = 5, 6, 7, \dots$$

The Brackett series start at $40500\overset{\circ}{\text{Å}}$ whereas the series limit lies at $14580\overset{\circ}{\text{Å}}$. The shortest or high frequency lines of Brackett series overlap with the Paschen series lines.

(v) **Pfund Series:** This series was discovered by A.H. Pfund in 1924 which corresponds to transition between the states with ($n_f = 5$) and successive higher states and lies in Infrared region of the spectrum.

$$\frac{1}{\lambda} = R \left(\frac{1}{5^2} - \frac{1}{n_i^2} \right) \quad n_i = 6, 7, 8, \dots$$

The Pfund series start at $74600\overset{\circ}{\text{Å}}$ whereas the series limit lies at $22790\overset{\circ}{\text{Å}}$.

(vi) **Humphreys Series:** The sixth series in the spectrum of hydrogen atom was observed by C.J. Humphreys in 1953 and lies in the infrared region of the spectrum. This series originates in transition to the sixth orbit from those of greater quantum numbers.

$$\frac{1}{\lambda} = R \left(\frac{1}{6^2} - \frac{1}{n_i^2} \right) \quad n_i = 7, 8, 9, \dots$$

The series with higher orders is unnamed but it follows the same rule given by J. Rydberg formula.