

Institute for NET/JRF, GATE, IIT-JAM, M.Sc. Entrance, JEST, TIFR and GRE in Physics

NET DECEMBER 2018

BOOKLET CODE 'A'

INSTRUCTIONS

- 1. You have opted for English as medium of question. This Test Booklet contains seventy five (20 Part 'A' +25 Part 'B' +30 Part 'C'). Multiple Choice Questions (MCQs).
 - You are required to answer a maximum of 15,20 and 20 questions from part 'A' 'B' and 'C' respectively. If more than required number of questions are answered, only first 15,20,20 questions in Part 'A' 'B' and 'C' respectively, will be taken up for evaluation.
- 2. **OMR** answer sheet has been provided separately. Before you start filling up your particulars, please ensure that the booklet contains requisite number of pages and that these are not torn or mutilated. If it is so, you may request the invigilator to change the booklet of the same code. Likewise check the **OMR** answer sheet also, Sheets for rough work have been appended to the test booklet.
- 3. Write your Roll No, Name and Serial Number of this Test Booklet on the **OMR** Answer sheet in the space provided. Also put your signatures in the space earn marked.
- 4. You must darken the appropriate circles with a black ball pen related to Roll Number, Subject Code, Booklet Code and Centre Code on the OMR answer sheet. It is the sole responsibility of the candidate to meticulously follow the instructions given on the answer sheet, failing which, the computer shall not be able to decipher the correct detail which may ultimately result in loss, including rejection of the OMR answer sheet.
- 5. Each question in Part 'A' carries 2 marks, Part 'B' 3.5 marks, Part 'C' 5 marks respectively. There will be negative marking @ 25% (Part 'A' 0.50 marks, Part 'B' 0.875 marks and Part 'C' 1.25 marks) for each wrong answer.
- 6. Below each question in Part 'A', 'B' and 'C' four alternative or responses are given. Only one of these alternatives is the "correct" option to the question. You have to find for each question, the correct or the best answer.
- 7. Candidate found copying or resorting to any unfair means are liable to be disqualified rough work.
- 8. Candidate should not write anything anywhere except on answer sheet of sheet for rough work.
- 9. Use of calculator is not permitted.
- 10. After the test is over, at the perforation point, tear the OMR answer sheet, hand over the original OMR answer sheet to the Invigator and retain the carbonless copy for your record.
- 11. Candidates who sit for the entire duration of the exam will only be permitted to carry their Test Booklet.



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PART A

Q1.	A rectangular photo frame of size $30 cm \times 40 cm$ has a photograph mounted at the cer			h mounted at the centre leaving		
	a 5cm border all around. The area of the border is					
	(a) $600 cm^2$	(b) $350 cm^2$	(c) $400 cm^2$	(d) $700 cm^2$		
Q2.	At a birthday party, o	every child gets 2 choo	colates, every mother g	gets 1 chocolate, while no father		
	gets a chocolate. In total 69 persons get 70 chocolates. If the number of children is half of the					
	number of mothers and fathers put together, then how many fathers are there?					
	(a) 22	(b) 23	(c) 24	(d) 69		
Q3.	What is the value of	$1^2 - 2^2 + 3^2 - 4^2 + 5^2$	$+17^2-18^2+19^2$?			
	(a) -5	(b) 12	(c) 95	(d) 190		
Q4.	The curves of $y = 2x^2$ and $y = 4x$ intersect each other at					
	(a) only one point		(b) exactly two points			
	(c) more than two points (d) no point at all					
Q5.	The diameters of th	The diameters of the pinholes of two otherwise identical cameras A and B are $500 \mu m$ and				
	$200 \mu m$, respectively	$200 \mu m$, respectively. Then the image in camera A will be				
	(a) sharper than in B		(b) darker than in B			
	(c) less sharp and brighter than in B		(d) sharper and brighter than in B			
Q6.	If $D = ABC + BCA + CAB$, where A, B and C are decimal digits, then D is divisible by					
	(a) 37 and 29		(b) 37 but not 29			
	(c) 29 but not 37		(d) neither 29 nor 37			
Q7.	For the following set of observed values {60,65,65,70,70,70,70,82,85,90,95,95,100,160,160}					
	which of the statements is true?					
	(a) mode < median < mean		(b) mode < mean < median			
	(c) mean < median <	mode	(d) median < mode < mean			
Q8.	A circular running track has six lanes, each $1m$ wide. How far ahead (in meters) should the					
	runner in the outermost lane start from, so as to cover the same distance in one lap as the runner					
	in the innermost lane?					
	(a) 6π	(b) 10π	(c) 12π	(d) 36π		

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Q9.	In an examination 100 questions of 1 mark each are given. After the examination, 20 questions			
	are deleted from evaluation, leaving 80 questions with a total of 100 marks. Student A had			
	answered 4 of the deleted questions correctly and got 40 marks, whereas student B had			
	answered 10 of the deleted questions correctly and got 35 marks. In this situation			
	(a) A and B were equally benefited (b) A and B lost equally			
	(c) B lost more than A (d) A lost more than B			
Q10.	ourist drives $20 km$ towards east, turns right and drives $6 km$, then drives $6 km$ towards west.			
	He then turns to his left and drives $4km$ and finally turns right and drives $14km$. Where is he			
	from his starting point?			
	(a) 6km towards east (b) 20km towards west			
	(c) 14km towards north (d) 10km towards south			
Q11.	If 'SELDOON' means 'NOODLES' then what does 'SPUOS' mean?			
	(a) SALAD (b) SOUPS (c) RASAM (d) ONION			
Q12.	An ideal pendulum oscillates with angular amplitude of 30° from the vertical. If it is observed at			
	a random instant of time, its angular deviation from the vertical is most likely to be			
	(a) 0^0 (b) $\pm 10^0$ (c) $\pm 20^0$ (d) $\pm 30^0$			
Q13.	the context of tiling a plane surface, which of the following polygons is the odd one out?			
	(a) Equilateral triangle (b) Square			
	(c) Regular pentagon (d) Regular hexagon			
Q14.	Scatter plots for pairs of observations on the variables x and y in samples A and B are shown			
	in the figure.			
	$y \times x \times y \times x \times y \times x \times x \times y$			
	y × ×			
	${}^{\times}_{\times}$ ${}^{\wedge}$ ${}^{\wedge}$ ${}^{\wedge}$ ${}^{\vee}$ ${}^{\vee}$			
	X X			
	Which of the following is suggested by the plots?			

- (a) Correlation between x and y is stronger in A than in B
- (b) Correlation between x and y is absent in B
- (c) Correlation between x and y is weaker in A than in B
- (d) y and x have a cause effect relationship in A but not in B



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- Q15. Two solutions X and Y containing ingredients A, B and C in proportions a:b:c and c:b:a, respectively, are mixed. For the resultant mixture to have A, B and C in equal proportion, it is necessary that
 - (a) $b = \frac{c-a}{2}$ (b) $c = \frac{a+b}{2}$ (c) $c = \frac{a-b}{2}$

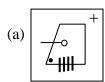
- Find the missing figure in the following sequence. Q16.





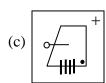








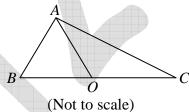








In triangle ABC, AB = 11, BC = 61, AC = 60, and O is the mid-point of BC. Then AO is



- (a) 18.5
- (b) 24.0
- (c) 30.5
- (d) 36.0
- Q18. Areas of three parts of a rectangle are given in unit of cm^2 . What is the total area of the rectangle?
 - (a) 18
 - (b) 24
 - (c) 36
 - (d) 108

9 6



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- Q19. A student is free to choose only Chemistry, only Biology or both. If out of 32 students, Chemistry has been chosen by 16 and Biology by 25, then how many students have chosen Biology but not Chemistry?
 - (a) 9

- (b) 16
- (c) 25
- (d) 7
- Q20. The lift (upward force due to air) generated by the wings and engines of an aircraft is
 - (a) positive (upwards) while landing and negative (downwards) while taking off.
 - (b) negative (downwards) while landing and positive (upwards) while taking off
 - (c) negative (downwards) while landing as well as while taking off
 - (d) positive (upwards) while landing as well as while taking off



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PART B

One of the eigenvalues of the matrix e^A is e^a , where $A = \begin{pmatrix} a & 0 & 0 \\ 0 & 0 & a \\ 0 & a & 0 \end{pmatrix}$. The product of the other

two eigenvalues of e^A is

- (d) 1
- The polynomial $f(x) = 1 + 5x + 3x^2$ is written as linear combination of the Legendre Q22. polynomials

 $\left(P_0(x) = 1, P_1(x), P_2(x) = \frac{1}{2}(3x^2 - 1)\right)$ as $f(x) = \sum_{n} c_n P_n(x)$. The value of c_0 is

- (a) $\frac{1}{4}$ (b) $\frac{1}{2}$ (c) 2 (d) 4

- The value of the integral $\oint_C \frac{dz}{z} \frac{\tanh 2z}{\sin \pi z}$, where C is a circle of radius $\frac{\pi}{2}$, traversed counter-Q23. clockwise, with centre at z = 0, is
 - (a) 4

- (b) 4i
- (c) 2i
- (d) 0
- A particle of mass m, moving along the x direction, experiences a damping force $-\gamma v^2$, where Q24. γ is a constant and ν is its instantaneous speed. If the speed at t=0 is ν_0 , the speed at time t is
- (b) $\frac{v_0}{1+\ln\left(1+\frac{\gamma v_0 t}{m}\right)}$ (c) $\frac{mv_0}{m+\gamma v_0 t}$ (d) $\frac{2v_0}{1+e^{\frac{\gamma v_0 t}{m}}}$

- The integral $I = \int_C e^z dz$ is evaluated from the point (-1,0) to (1,0)Q25. along the contour C, which is an arc of the parabola $y = x^2 - 1$, as (-1,0)shown in the figure.

Re z.

The value of I is

(a) 0

- (b) $2 \sinh 1$ (c) $e^{2i} \sinh 1$ (d) $e + e^{-1}$



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Q26. In terms of arbitrary constants A and B, the general solution to the differential equation

$$x^{2} \frac{d^{2}y}{dx^{2}} + 5x \frac{dy}{dx} + 3y = 0$$
 is

(a)
$$y = \frac{A}{x} + Bx^3$$

(b)
$$y = Ax + \frac{B}{x^3}$$

(c)
$$y = Ax + Bx^3$$

(d)
$$y = \frac{A}{x} + \frac{B}{x^3}$$

In the attractive Kepler problem described by the central potential $V(r) = \frac{-k}{r}$ (where k is a Q27. positive constant), a particle of mass m with a non-zero angular momentum can never reach the centre due to the centrifugal barrier. If we modify the potential to

$$V(r) = -\frac{k}{r} - \frac{\beta}{r^3}$$

one finds that there is a critical value of the angular momentum ℓ_c below which there is no centrifugal barrier. This value of ℓ_c is

(a)
$$\left[12km^2\beta\right]^1$$

(b)
$$\left[12km^2\beta\right]^{-1}$$

(c)
$$\left[12km^2\beta\right]^{1/2}$$

(a)
$$\left[12km^{2}\beta\right]^{1/2}$$
 (b) $\left[12km^{2}\beta\right]^{-1/2}$ (c) $\left[12km^{2}\beta\right]^{1/4}$ (d) $\left[12km^{2}\beta\right]^{-1/4}$

The time period of a particle of mass m, undergoing small oscillations around x = 0, in the Q28. potential $V = V_0 \cosh\left(\frac{x}{L}\right)$, is

(a)
$$\pi \sqrt{\frac{mL^2}{V_0}}$$

(b)
$$2\pi \sqrt{\frac{mL^2}{2V_0}}$$

(c)
$$2\pi\sqrt{\frac{mL^2}{V_0}}$$

(a)
$$\pi \sqrt{\frac{mL^2}{V_0}}$$
 (b) $2\pi \sqrt{\frac{mL^2}{2V_0}}$ (c) $2\pi \sqrt{\frac{mL^2}{V_0}}$ (d) $2\pi \sqrt{\frac{2mL^2}{V_0}}$

Consider the decay $A \to B + C$ of a relativistic spin- $\frac{1}{2}$ particle A. Which of the following Q29. statements is true in the rest frame of the particle A?

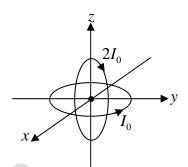
- (a) The spin of both B and C may be $\frac{1}{2}$
- (b) The sum of the masses of B and C is greater than the mass of A
- (c) The energy of B is uniquely determined by the masses of the particles
- (d) The spin of both B and C may be integral



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Q30. Two current-carrying circular loops, each of radius R, are placed perpendicular to each other, as shown in the figure.

The loop in the xy- plane carries a current I_0 while that in the xz -plane carries a current $2I_0$. The resulting magnetic field \vec{B} at the origin is



+q(L,b)

-q(L,-b)

(a)
$$\frac{\mu_0 l_0}{2R} \left[2\hat{j} + \hat{k} \right]$$

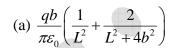
(b)
$$\frac{\mu_0 l_0}{2R} \left[2\hat{j} - \hat{k} \right]$$

(c)
$$\frac{\mu_0 l_0}{2R} \left[-2\hat{j} + \hat{k} \right]$$

$$(d)\frac{\mu_0 l_0}{2R} \left[-2\hat{j} - \hat{k} \right]$$

An electric dipole of dipole moment $\vec{P} = qb\hat{i}$ is placed at Q31. origin in the vicinity of two charges +q and -q at (L,b)and (L,-b), respectively, as shown in the figure.

The electrostatic potential at the point $\left(\frac{L}{2},0\right)$ is

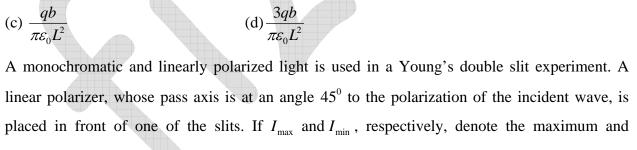


(b)
$$\frac{4qbL}{\pi\varepsilon_0 \left[L^2 + 4b^2\right]^{3/2}}$$

(c)
$$\frac{qb}{\pi \varepsilon_0 L^2}$$

Q32.

(d)
$$\frac{3qb}{\pi \varepsilon_0 L^2}$$



minimum intensities of the interference pattern on the screen, the visibility, defined as the ratio

$$\frac{I_{\text{max}} - I_{\text{min}}}{I_{\text{max}} + I_{\text{min}}}, \text{ is}$$

(a)
$$\frac{\sqrt{2}}{3}$$

(b)
$$\frac{2}{3}$$

(c)
$$\frac{2\sqrt{2}}{3}$$

(d)
$$\sqrt{\frac{2}{3}}$$



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Q33. An electromagnetic wave propagates in a nonmagnetic medium with relative permittivity $\varepsilon = 4$. The magnetic field for this wave is

$$\vec{H}(x,y) = \hat{k}H_0 \cos(\omega t - \alpha x - \alpha \sqrt{3}y)$$

where H_0 is a constant. The corresponding electric field $\vec{E}(x, y)$ is

(a)
$$\frac{1}{4}\mu_0 H_0 c \left(-\sqrt{3}\hat{i} + \hat{j}\right) \cos\left(\omega t - \alpha x - \alpha\sqrt{3}y\right)$$

(b)
$$\frac{1}{4}\mu_0 H_0 c \left(\sqrt{3}\hat{i} + \hat{j}\right) \cos\left(\omega t - \alpha x - \alpha\sqrt{3}y\right)$$

(c)
$$\frac{1}{4}\mu_0 H_0 c \left(\sqrt{3}\hat{i} - \hat{j}\right) \cos\left(\omega t - \alpha x - \alpha\sqrt{3}y\right)$$

(d)
$$\frac{1}{4}\mu_0 H_0 c \left(-\sqrt{3}\hat{i} - \hat{j}\right) \cos\left(\omega t - \alpha x - \alpha\sqrt{3}y\right)$$

- The ground state energy of an anisotropic harmonic oscillator described by the potential Q34. $V(x, y, z) = \frac{1}{2}m\omega^2 x^2 + 2m\omega^2 y^2 + 8m\omega^2 z^2$ (in units of $\hbar\omega$) is
 - (a) $\frac{5}{2}$

- The product $\Delta x \Delta p$ of uncertainties in the position and momentum of a simple harmonic Q35. oscillator of mass m and angular frequency ω in the ground state $|0\rangle$, is $\frac{\hbar}{2}$. The value of the product $\Delta x \Delta p$ in the state, $e^{-i\hat{p}\ell/\hbar}|0\rangle$ (where ℓ is a constant and \hat{p} is the momentum operator) is
 - (a) $\frac{\hbar}{2} \sqrt{\frac{m\omega\ell^2}{\hbar}}$ (b) \hbar

- (c) $\frac{\hbar}{2}$
- (d) $\frac{\hbar^2}{mc^{\ell^2}}$
- Let the wavefunction of the electron in a hydrogen atom be Q36.

$$\psi(\vec{r}) = \frac{1}{\sqrt{6}}\phi_{200}(\vec{r}) + \sqrt{\frac{2}{3}}\phi_{21-1}(\vec{r}) - \frac{1}{\sqrt{6}}\phi_{100}(\vec{r})$$

where $\phi_{nlm}(\vec{r})$ are the eigenstates of the Hamiltonian in the standard notation. The expectation value of the energy in this state is

- (a) $-10.8 \ eV$
- (b) $-6.2 \ eV$
- (c) $-9.5 \, eV$
- (d) $-5.1 \, eV$



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- Three identical spin $\frac{1}{2}$ particles of mass m are confined to a one-dimensional box of length L, but are otherwise free. Assuming that they are non-interacting, the energies of the lowest two energy eigen states, in units of $\frac{\pi^2 \hbar^2}{2mL^2}$, are
 - (a) 3 and 6
- (b) 6 and 9
- (c) 6 and 11
- (d) 3 and 9
- The heat capacity C_V at constant volume of a metal, as a function of temperature, is $\alpha T + \beta T^3$, Q38. where α and β are constants. The temperature dependence of the entropy at constant volume is
 - (a) $\alpha T + \frac{1}{2}\beta T^3$

(c) $\frac{1}{2} \alpha T + \frac{1}{3} \beta T^3$

- (b) $\alpha T + \beta T^3$ (d) $\frac{1}{2}\alpha T + \frac{1}{4}\beta T^3$
- The rotational energy levels of a molecule are $E_{\ell} = \frac{\hbar^2}{2I_{\ell}} \ell(\ell+1)$, where $\ell = 0,1,2,...$ and I_0 is its Q39. moment of inertia. The contribution of the rotational motion to the Helmholtz free energy per molecule, at low temperatures in a dilute gas of these molecules, is approximately
 - (a) $-k_BT\left(1+\frac{\hbar^2}{I_0k_BT}\right)$

 $(c) -k_B T$

- (b) $-k_B T e^{-\frac{\hbar^2}{I_0 k_B T}}$ (d) $-3k_B T e^{-\frac{\hbar^2}{I_0 k_B T}}$
- Q40. The vibrational motion of a diatomic molecule may be considered to be that of a simple harmonic oscillator with angular frequency ω . If a gas of these molecules is at temperature T, what is the probability that a randomly picked molecule will be found in its lowest vibrational state?
 - (a) $1-e^{-\frac{\hbar\omega}{k_BT}}$

(b) $e^{-\frac{\hbar\omega}{2k_BT}}$

(c) $\tanh\left(\frac{\hbar\omega}{k_BT}\right)$

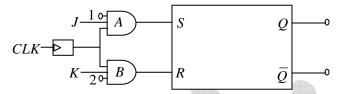
(d) $\frac{1}{2}$ cosec $h\left(\frac{\hbar\omega}{2k_BT}\right)$



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- O41. Consider an ideal Fermi gas in a grand canonical ensemble at a constant chemical potential. The variance of the occupation number of the single particle energy level with mean occupation number \overline{n} is
 - (a) $\overline{n}(1-\overline{n})$ (b) $\sqrt{\overline{n}}$
- (c) \overline{n}
- (d) $\frac{1}{\sqrt{\overline{n}}}$
- Consider the following circuit, consisting of an RS flip-flop and two AND gates. Q42.



Which of the following connections will allow the entire circuit to act as a JK flip-flop?

- (a) connect Q to pin 1 and \overline{Q} to pin 2
- (b) connect Q to pin 2 and \overline{Q} to pin 1
- (c) connect Q to K input and \overline{Q} to J input
- (d) connect Q to J input and \overline{Q} to K input
- Q43. The truth table below gives the value Y(A, B, C) where A, B and C are binary variables.

The output Y can be represented by

(a)
$$Y = \overline{ABC} + \overline{ABC} + A\overline{BC} + A\overline{BC} + AB\overline{C}$$

(b)
$$Y = \overline{ABC} + \overline{ABC} + A\overline{BC} + ABC$$

(c)
$$Y = \overline{ABC} + \overline{ABC} + A\overline{BC} + ABC$$

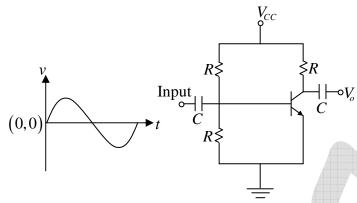
(d)
$$Y = \overline{A}\overline{B}\overline{C} + \overline{A}\overline{B}\overline{C} + A\overline{B}\overline{C} + AB\overline{C}$$

A	В	C	Y
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	1
1	1	0	0
1	1	1	1

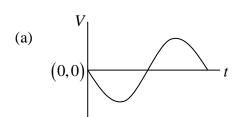


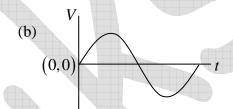
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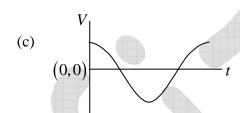
Q44. A sinusoidal signal is an input to the following circuit

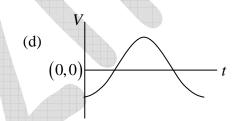


Which of the following graphs best describes the output wave function?



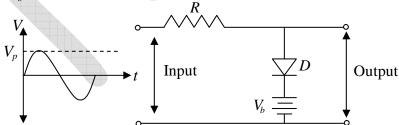






Q45. A sinusoidal voltage having a peak value of V_p is an input to the following circuit, in which the

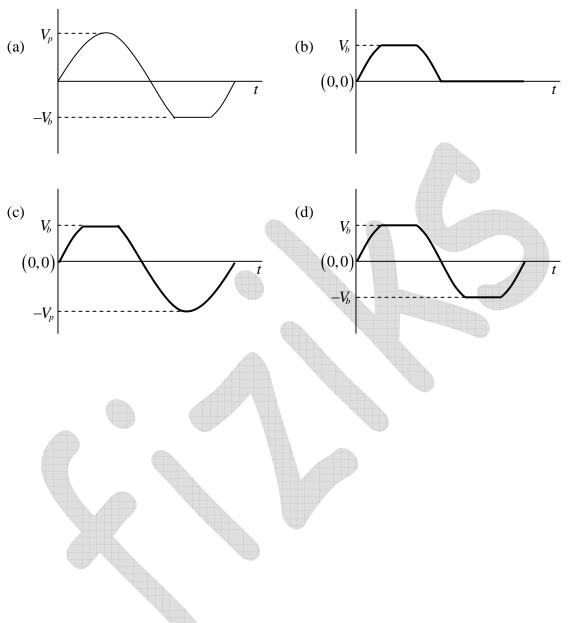
DC voltage is V_b





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Assuming an ideal diode which of the following best describes the output waveform?





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PART C

Q46. The Green's function G(x, x') for the equation $\frac{d^2y(x)}{dx^2} = f(x)$, with the boundary values y(0) = 0 and y(1) = 0, is

(a)
$$G(x,x') = \begin{cases} \frac{1}{2}x(1-x'), & 0 < x < x' < 1 \\ \frac{1}{2}x'(1-x), & 0 < x' < x < 1 \end{cases}$$
 (b) $G(x,x') = \begin{cases} x(x'-1), & 0 < x < x' < 1 \\ x'(1-x), & 0 < x' < x < 1 \end{cases}$

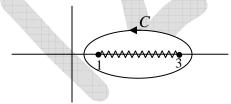
(c)
$$G(x,x') = \begin{cases} -\frac{1}{2}x(1-x'), & 0 < x < x' < 1\\ \frac{1}{2}x'(1-x), & 0 < x' < x < 1 \end{cases}$$
 (d) $G(x,x') = \begin{cases} x(x'-1), & 0 < x < x' < 1\\ x'(x-1), & 0 < x' < x < 1 \end{cases}$

- Q47. A 4×4 complex matrix A satisfies the relation $A^{\dagger}A=4I$, where I is the 4×4 identity matrix. The number of independent real parameters of A is
 - (a) 32
- (b) 10
- (c) 12
- (d) 16

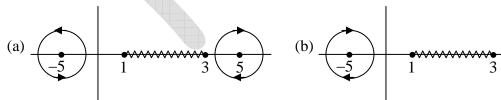
Q48. The contour C of the following integral

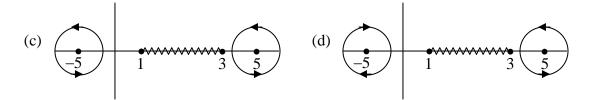
$$\oint_C dz \frac{\sqrt{(z-1)(z-3)}}{\left(z^2-25\right)^3}$$

in the complex z plane is shown in the figure below.



This integral is equivalent to an integral along the contours







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Q49.	The value of the integral $\int_0^1 x^2 dx$, evaluated using the trapezoidal rule with a step size of 0.2, is				
	(a) 0.30	(b) 0.39	(c) 0.34	(d) 0.27	
Q50.	The motion of a part	icle in one dimension	is described by the La	angrangian $L = \frac{1}{2} \left(\left(\frac{dx}{dt} \right)^2 - x^2 \right)$	
	in suitable units. The	value of the action al	ong the classical path	from $x = 0$ at $t = 0$ to $x = x_0$ at	
	$t=t_0$, is				
	(a) $\frac{x_0^2}{2\sin^2 t_0}$	(b) $\frac{1}{2}x_0^2 \tan t_0$	$(c) \frac{1}{2} x_0^2 \cot t_0$	(d) $\frac{x_0^2}{2\cos^2 t_0}$	
Q51.	The Hamiltonian of	a classical one-dime	ensional harmonic osc	cillator is $H = \frac{1}{2}(p^2 + x^2)$, in	
	suitable units. The total time derivative of the dynamical variable $(p + \sqrt{2}x)$ is				
	(a) $\sqrt{2}p-x$	(b) $p - \sqrt{2}x$	(c) $p + \sqrt{2}x$	(d) $x + \sqrt{2}p$	
Q52.	A relativistic particle	e of mass m and charge	ge e is moving in a ur	niform electric field of strength	
	ε . Starting from rest at $t = 0$, how much time will it take to reach the speed $\frac{c}{2}$?				
	(a) $\frac{1}{\sqrt{3}} \frac{mc}{e\varepsilon}$	(b) $\frac{mc}{e\varepsilon}$	$(c)\sqrt{2}\frac{mc}{e\varepsilon}$	(d) $\sqrt{\frac{3}{2}} \frac{mc}{e\varepsilon}$	
Q53.	In an inertial frame u	niform electric and ma	agnetic field \vec{E} and \vec{B}	are perpendicular to each other	
	and satisfy $ \vec{E} ^2 - \vec{B} ^2 = 29$ (in suitable units). In another inertial frame, which moves at a constant				
	velocity with respect to the first frame, the magnetic field is $2\sqrt{5}\hat{k}$. In the second frame, an				
	electric field consistent with the previous observations is				
	(a) $\frac{7}{\sqrt{2}}(\hat{i}+\hat{j})$	(b) $7(\hat{i} + \hat{k})$	(c) $\frac{7}{\sqrt{2}}(\hat{i}+\hat{k})$	(d) $7(\hat{i} + \hat{j})$	
Q54.				a medium in which, over a band	
	of frequencies the re-	equencies the refractive index is $n(\omega) \approx 1 - \left(\frac{\omega}{\omega_0}\right)^2$, where ω_0 is a constant. The ratio $\frac{v_g}{v_p}$ of			
	the group velocity to the phase velocity at $\omega = \frac{\omega_0}{2}$ is				
	(a) 3	(b) $\frac{1}{4}$	(c) $\frac{2}{3}$	(d) 2	



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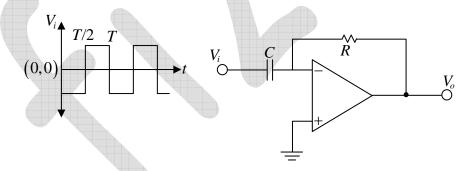
Q55.	A rotating spherical shell of uniform surface charge and mass density has total mass M				
	charge Q . If its angular momentum is L and magnetic moment is μ , then the ratio $\frac{\mu}{L}$ is			μ , then the ratio $\frac{\mu}{L}$ is	
	(a) $\frac{Q}{3M}$	(b) $\frac{2Q}{3M}$	(c) $\frac{Q}{2M}$	(d) $\frac{3Q}{4M}$	
Q56.	Consider the operator	or $A_x = L_y p_z - L_z p_y$, w	where L_i and p_i denote	e, respectively, the components	
	of the angular momentum and momentum operators. The commutator $[A_x, x]$, where x i x - component of the position operator, is				
		(b) $-i\hbar \left(zp_z - yp_y\right)$			
Q57.	A one-dimensional s	system is described by	V the Hamiltonian $H = \frac{1}{2}$	$= \frac{p^2}{zm} + \lambda x \text{ (where } \lambda > 0 \text{). The}$	
	ground state energy varies as a function of λ as				
	(a) $\lambda^{5/3}$	(b) $\lambda^{2/3}$	(c) $\lambda^{4/3}$	(d) $\lambda^{1/3}$	
Q58.	If the position of the electron in the ground state of a Hydrogen atom is measured, the probabili			om is measured, the probability	
	that it will be found at a distance $r \ge a_0$ (a_0 being Bohr radius) is nearest to				
	(a) 0.91	(b) 0.66	(c) 0.32	(d) 0.13	
Q59.	A system of spin $\frac{1}{2}$	particles is prepared to	o be in the eigenstate	of σ_z with eigenvalue +1. The	
	system is rotated by at angle of 60° about the x-axis. After the rotation, the fraction of the particles that will be measured to be in the eigenstate of σ_z with eigenvalue +1 is				
	(a) $\frac{1}{3}$	(b) $\frac{2}{3}$	(c) $\frac{1}{4}$	(d) $\frac{3}{4}$	
Q60.	The Hamiltonian of a	a one-dimensional Ising	g model of N spins (I	V large) is	
	$H=-J\sum_{i=1}^N\sigma_i\sigma_{i+1}$ where the spin $\sigma_i=\pm 1$ and J is a positive constant. At inverse temperature $\beta=\frac{1}{k_BT}$, the				
	correlation function b	correlation function between the nearest neighbor spins $(\sigma_i \sigma_{i+1})$ is			
	(a) $\frac{e^{-\beta J}}{\left(e^{\beta J} + e^{-\beta J}\right)}$	(b) $e^{-2\beta J}$	(c) $\tanh(\beta J)$	$(d) \coth(\beta J)$	



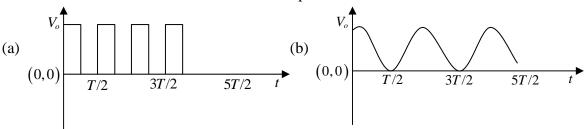
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- Q61. At low temperatures, in the Debye approximation, the contribution of the phonons to the heat capacity of a two dimensional solid is proportional to
 - (a) T^2
- (b) T^3
- (c) $T^{1/2}$
- (d) $T^{3/2}$
- Q62. A particle hops on a one-dimensional lattice with lattice spacing a. The probability of the particle to hop to the neighboring site to its right is p, while the corresponding probability to hop to the left is q = 1 - p. The root-mean squared deviation $\Delta x = \sqrt{\langle x^2 \rangle - \langle x \rangle^2}$ in displacement after N steps, is
 - (a) $a\sqrt{Npq}$
- (b) $aN\sqrt{pq}$

- The energy levels accessible to a molecule have energies $E_1 = 0$, $E_2 = \Delta$ and $E_3 = 2\Delta$ (where Δ Q63. is a constant). A gas of these molecules is in thermal equilibrium at temperature T. The specific heat at constant volume in the high temperature limit $(k_B T \gg \Delta)$ varies with temperature as
 - (a) $\frac{1}{T^{3/2}}$
- (b) $\frac{1}{T^3}$
- (c) $\frac{1}{T}$ (d) $\frac{1}{T^2}$
- The input V_i to the following circuit is a square wave as shown in the following figure. Q64.

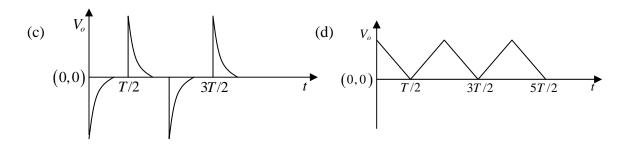


which of the waveforms best describes the output?

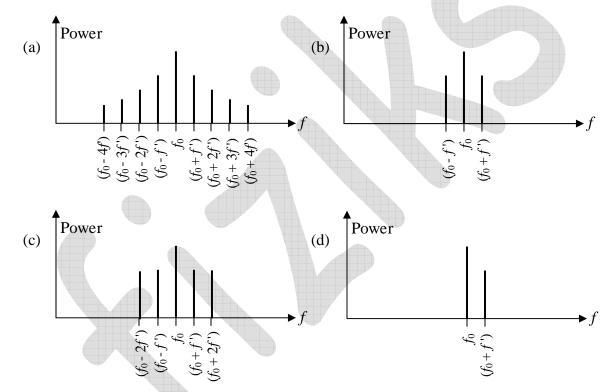




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Q65. The amplitude of a carrier signal of frequency f_0 is sinusoidally modulated at a frequency $f' \ll f_0$. Which of the following graphs best describes its power spectrum?



Q66. The standard deviation of the following set of data $\{10.0, 10.0, 9.9, 9.9, 9.8, 9.9, 9.9, 9.9, 9.8, 9.9\}$ is nearest to

- (a) 0.10
- (b) 0.07
- (c) 0.01
- (d) 0.04

Q67. The diatomic molecule HF has an absorption line in the rotational band at 40 cm^{-1} for the isotope ^{18}F . The corresponding line for the isotope ^{19}F will be shifted by approximately

- (a) $0.05 cm^{-1}$
- (b) $0.11cm^{-1}$
- (c) $0.33 \ cm^{-1}$
- (d) $0.01 \ cm^{-1}$



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The excited state (n = 4, l = 2) of an election in an atom may decay to one or more of the lower Q68. energy levels shown in the diagram below.

$$n = 4 \frac{1}{l = 2}$$

$$n=3$$
 $\frac{1}{l=0}$ $\frac{1}{l=1}$ $\frac{1}{l=2}$

$$n=2\frac{1}{l=1}$$

Of the total emitted light, a fraction $\frac{1}{4}$ comes from the decay to the state (n=2,l=1). Based on selection rules, the fractional intensity of the emission line due to the decay to the state (n = 3, l = 1)

- (a) $\frac{3}{4}$
- (b) $\frac{1}{2}$
- (c) $\frac{1}{4}$

(d)0

The volume of an optical cavity is $1 cm^3$. The number of modes it can support within a Q69. bandwidth of 0.1 nm, centered at $\lambda = 500$ nm, is of the order of

- (a) 10^3
- $(b)10^5$
- $(c)10^{10}$
- (d) 10^7

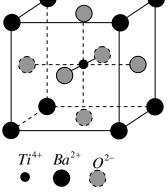
Barium Titanate (BaTiO₃) crystal has a cubic perovskite structure, Q70. where the Ba^{2+} ions are at the vertices of a unit cube, the O^{2-} ions are at the centres of the faces while the Ti^{2+} is at the centre. The number of optical phonon modes of the crystal is

(a) 12

(b)15

(c) 5

(d)18



The dispersion relation of optical phonons in a cubic crystal is given by $\omega(k) = \omega_0 - ak^2$ where Q71. ω_0 and a are positive constants. The contribution to the density of states due to these phonons with frequencies just below ω_0 is proportional to

- (a) $(\omega_0 \omega)^{1/2}$ (b) $(\omega_0 \omega)^{3/2}$ (c) $(\omega_0 \omega)^2$ (d) $(\omega_0 \omega)$



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- A silicon crystal is doped with phosphorus atoms. (The binding energy of a H atom is 13.6 eV, Q72. the dielectric constant of silicon is 12 and the effective mass of electrons in the crystal is $0.4 m_e$). The gap between the donor energy level and the bottom of the conduction band is nearest to
 - (a) $0.01 \, eV$
- (b) $0.08 \ eV$
- (c) 0.02 eV
- (d) $0.04 \ eV$
- Q73. Assume that pion-nucleon scattering at low energies, in which isospin is conserved is described by the effective interaction potential $V_{eff} = F(r)\vec{I}_{\pi}.\vec{I}_{N}$, where F(r) is a function of the radial separation r and \vec{I}_{π} and \vec{I}_{N} denote, respectively, the isospin vectors of a pion and the nucleon.

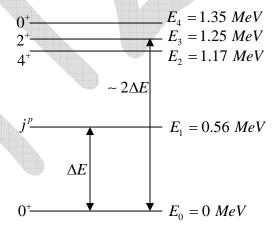
The ratio $\frac{\sigma_{I=3/2}}{\sigma_{I=1/2}}$ of the scattering cross-sections corresponding to total isospins $I=\frac{3}{2}$ and $\frac{1}{2}$ is

- (b) $\frac{1}{4}$ (c) $\frac{5}{4}$
- (d) $\frac{1}{2}$
- Q74. A nucleus decays by the emission of a gamma ray from an excited state of spin parity 2⁺ to the ground state with spin-parity 0^+ what is the type of the corresponding radiation?
 - (a) magnetic dipole

(b) electric quadrupole

(c) electric dipole

- (d) magnetic quadrupole
- The low lying energy levels due to the vibrational excitations of an even-even nucleus are shown O75. in the figure below.



The spin-parity j^p of the level E_1 is

(a) 1^{+}

- (b) 1⁻
- (c) 2^{-}
- (d) 2^{+}